

Robust Project

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Analysis of test data from European laboratories

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1 Introduction

This document contains the results of activities conducted inside Work Package (WP) 2 of the ROBUST project.

The basic purpose of this task was as follows:

- Analysis of existing data obtained from European laboratories to investigate any possible correlation between severity indices and performance criteria.
- Analysis of existing data obtained from European laboratories to investigate any differences between tests houses, based on existing data.
- Application of the results obtained in WP3 to a set of raw data obtained from EU laboratories.
- Correlation between barrier performance and biomechanics criteria.

2 Analysis of existing data obtained from European laboratories

A collection of 174 data sets from full scale TB11 crash tests have been obtained from European laboratories. They contained the following information:

- year of test
- vehicle make
- vehicle test mass
- data sample rate
- actual speed and angle
- barrier dynamic deflection
- ASI
- THIV/PHD

Data was received from seven Laboratories. Of the 174 TB11 tests, 111 were successful and 63 unsuccessful. Some tests have been received without PHD data. Data have been reported (in an anonymous format) at the end of this document.

In the following table the test houses that provided these test data have been identified:

LABORATORY	Number of tests
Autostrade	31
BAST	24
Finland	1
LIER	80
MIRA	1
TRL	9
VTI	28

Table 1. Test results analysed

2.1 Compliance with severity criteria

63 of the 174 tests failed at least one of the severity criteria. Only 14 (22%) failed both criteria; 21 (33%) failed ASI only and 28 (45%) failed THIV/PHD only

42 tests failed the THIV/PHD criterion; 13 failed by THIV alone, 25 by PHD alone and only 4 by both.

COMPLIANCE		THIV/PHD		
		PASS	FAIL	TOTAL
ASI	PASS	111	28	139
	FAIL	21	14	35
	TOTAL	132	42	174

Table 2: Severity indices distribution

2.2 Correlation between ASI, THIV and PHD

A series of correlation analyses have been performed between the data sets made available by the test laboratories. In the following figures some of these are examined.

A first comparison is made between THIV and ASI values:

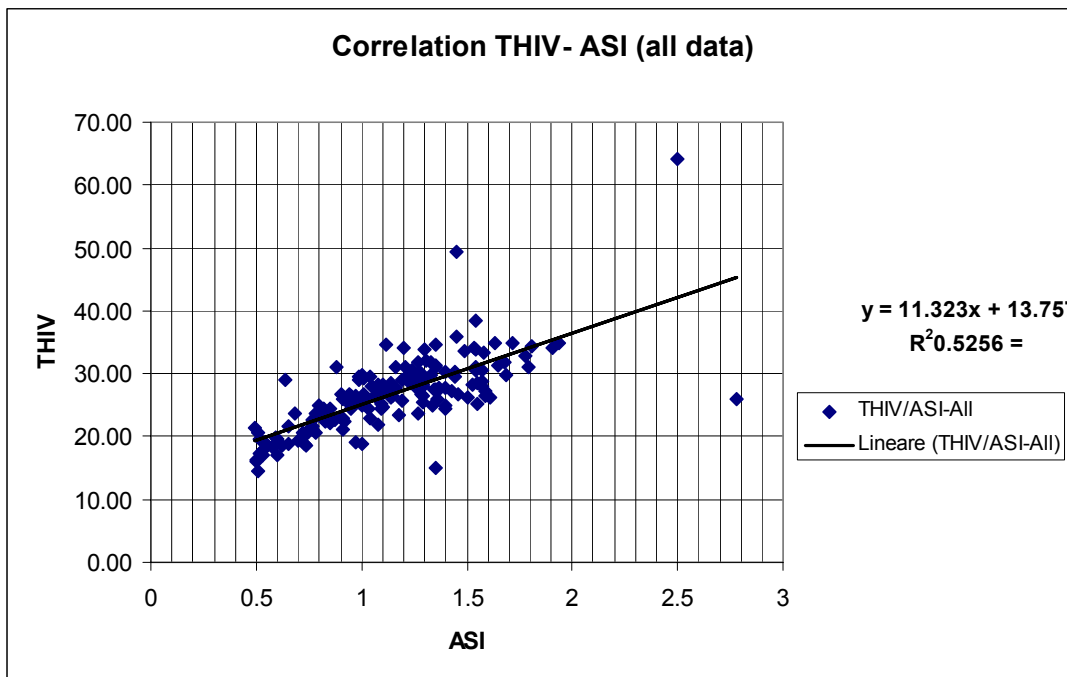


Figure 1: THIV_ASI correlation.

The above figure contains some singular results that have been removed to obtain the following figure:

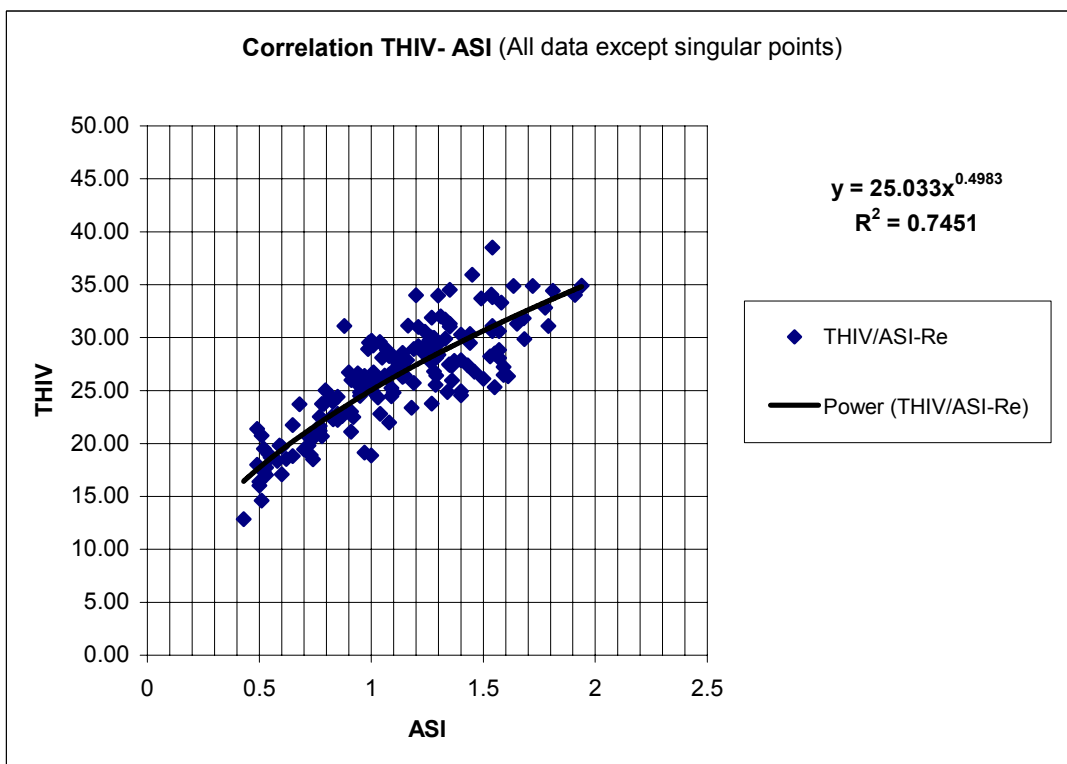


Figure 2: THIV ASI correlation.

This graph shows a fair correlation between ASI and THIV indices.

A further comparison is made to investigate the tendencies between the different laboratories. This comparison has been made between laboratories that have provided more than one data set:

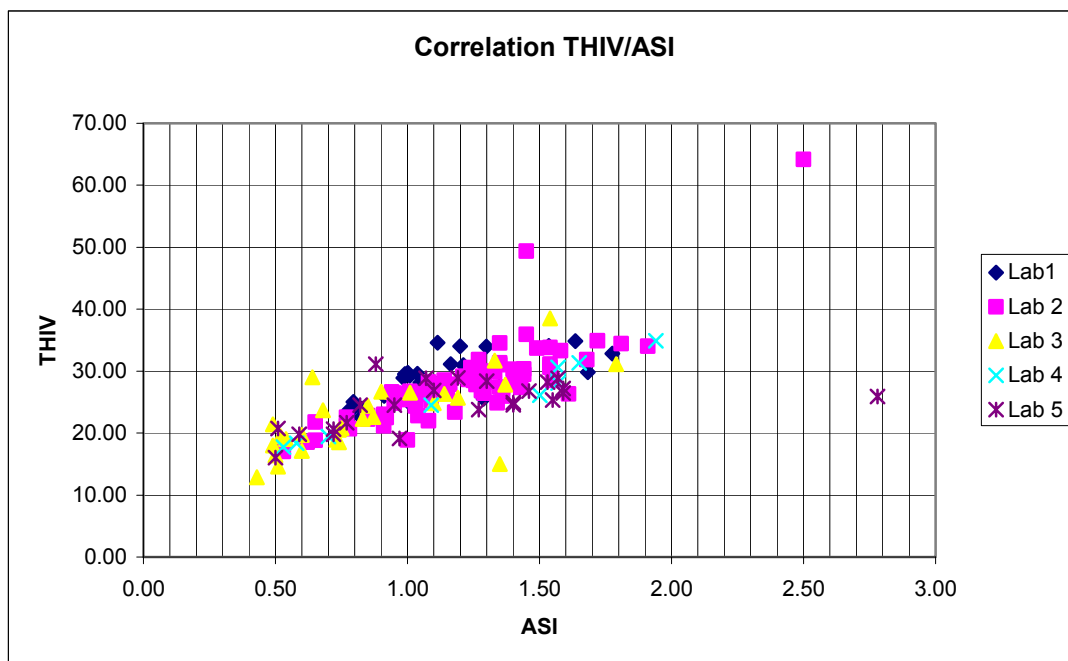


Figure 3: ASI to THIV correlation within different Laboratories.

It can be seen that, apart from the singular points, the tendencies between the different labs are similar. This can also be seen in the following table reporting the correlation functions for different laboratories.

Lab	Corr. function
ALL	$y = 25.033x^{0.4983}$
1	$y = 26.981x^{0.4305}$
2	$y = 24.018x^{0.3305}$
3	$y = 24.787x^{0.545}$
4	$y = 25.088x^{0.5596}$
5	$y = 23.637x^{0.4899}$

Table 3: ASI-THIV correlation functions

From Figure 2 it can be seen that the best correlation function is the following:

$$THIV = 25.033 \cdot ASI^{0.4989}$$

This equation has a correlation factor (R^2) of 0.7451.

This correlation function creates the following table:

ASI	THIV
1.0	25.033

1.4	29.61
-----	-------

Table 4: ASI THIV

It should be noted that at present, within EN1317-2, the current threshold value for THIV is quoted as 33kph.

The following graphs investigate the relationship between THIV and PHD, and between PHD and ASI:

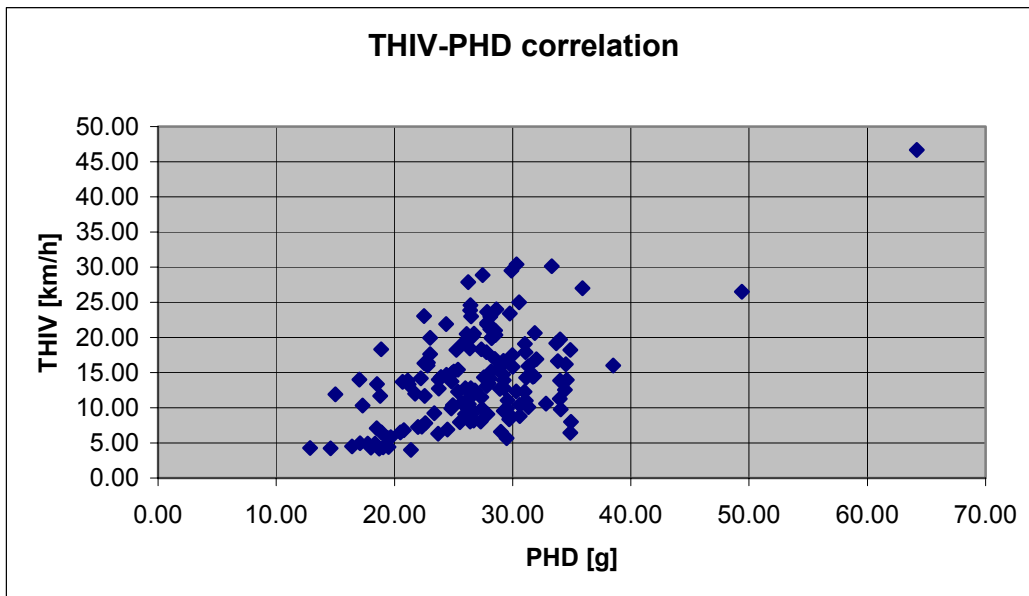


Figure 4: THIV and PHD correlation

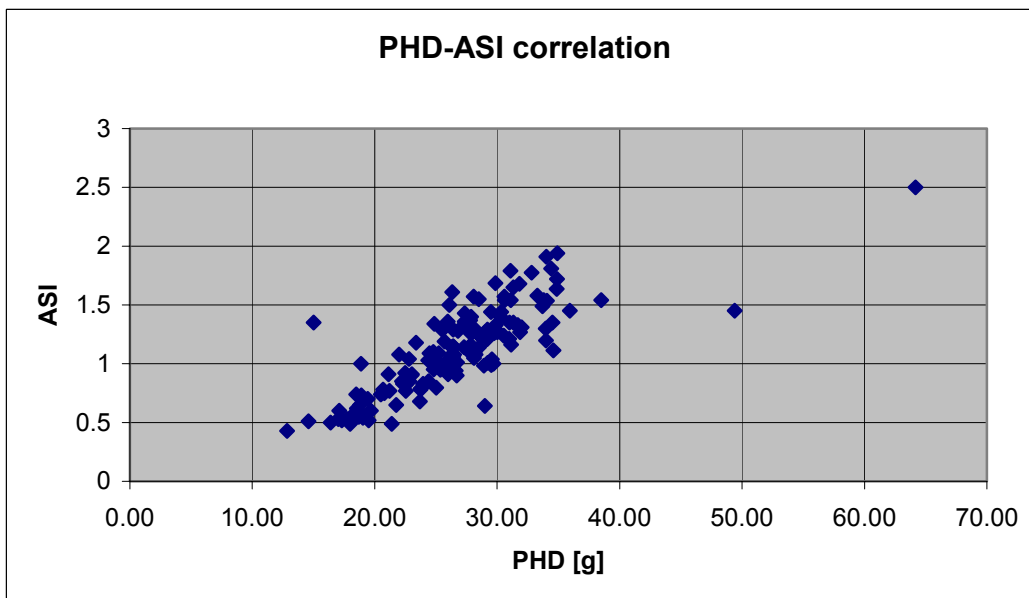


Figure 5: PHD and ASI correlation

The above results show no correlation between PHD and THIV or ASI.

2.3 Correlation between Dynamic deflection and severity indices

In the following figure, the correlation between severity indices and dynamic deflection is investigated:

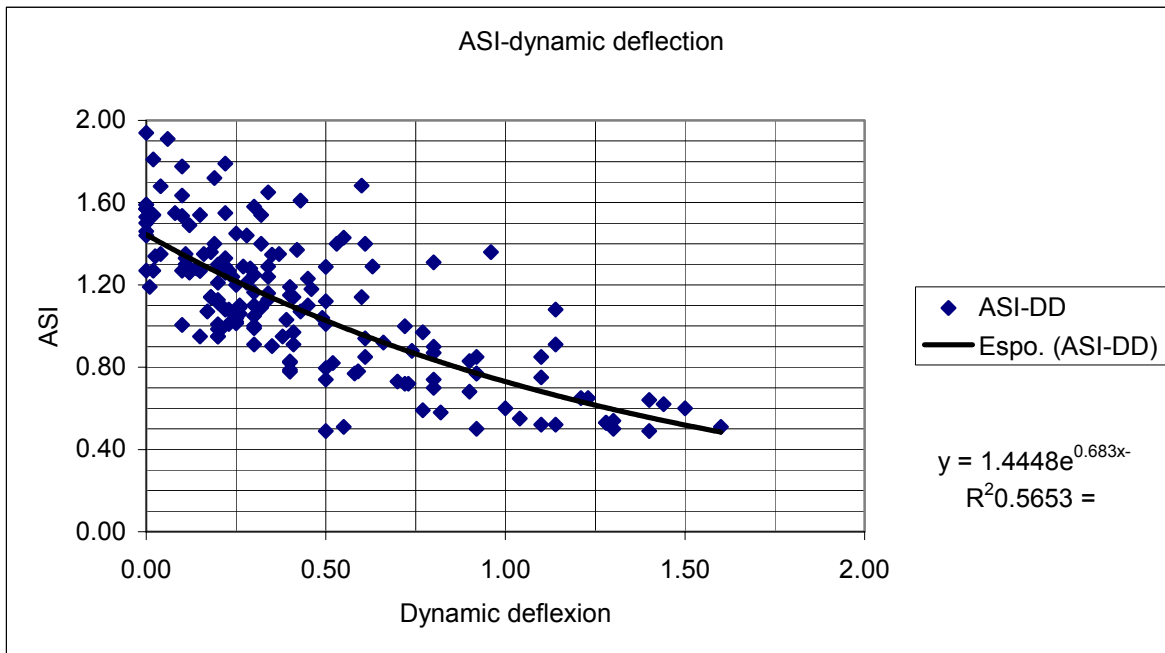


Figure 6: ASI and dynamic deflection correlation.

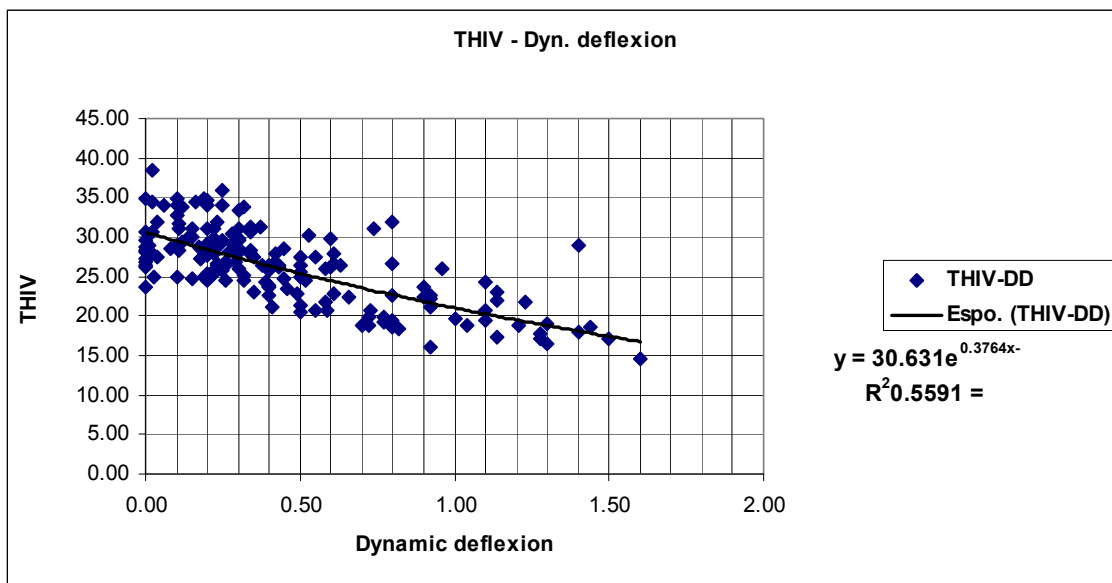


Figure 7: THIV and dynamic deflection correlation

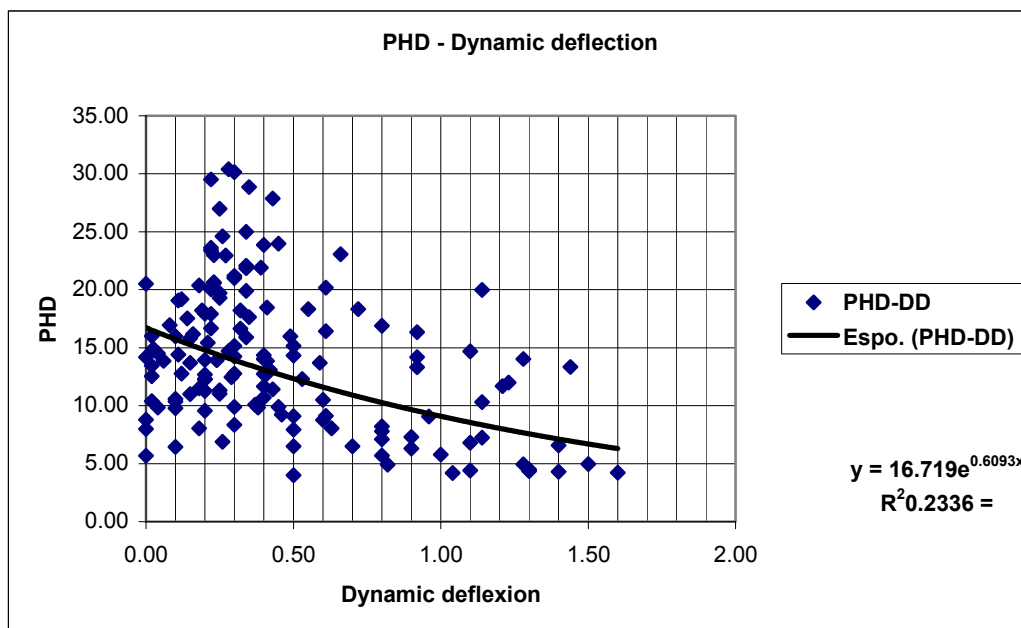


Figure 8: PHD and dynamic deflection correlation

The investigation shows a weak correlation between THIV, ASI and dynamic deflection and no correlation between PHD and dynamic deflection.

The correlation between ASI, THIV and dynamic deflection has again been analysed to investigate any different tendencies between the different laboratories.

These results show that there is only a very limited correlation between severity indices. It has already been demonstrated on previous occasions that from a scientific point of view, ASI, THIV and PHD are different things, and this is enough to explain the lack of correlation in many cases.

The main differences between the severity indices are:

- ASI uses three components of acceleration while THIV-PHD use a planar motion where the z acceleration component is not used.
- THIV – PHD use a critical time that corresponds to the time where the theoretical head impact against the conventional box representing the vehicle interior.
- THIV is affected by the yaw motion while ASI does not take this measure into account.

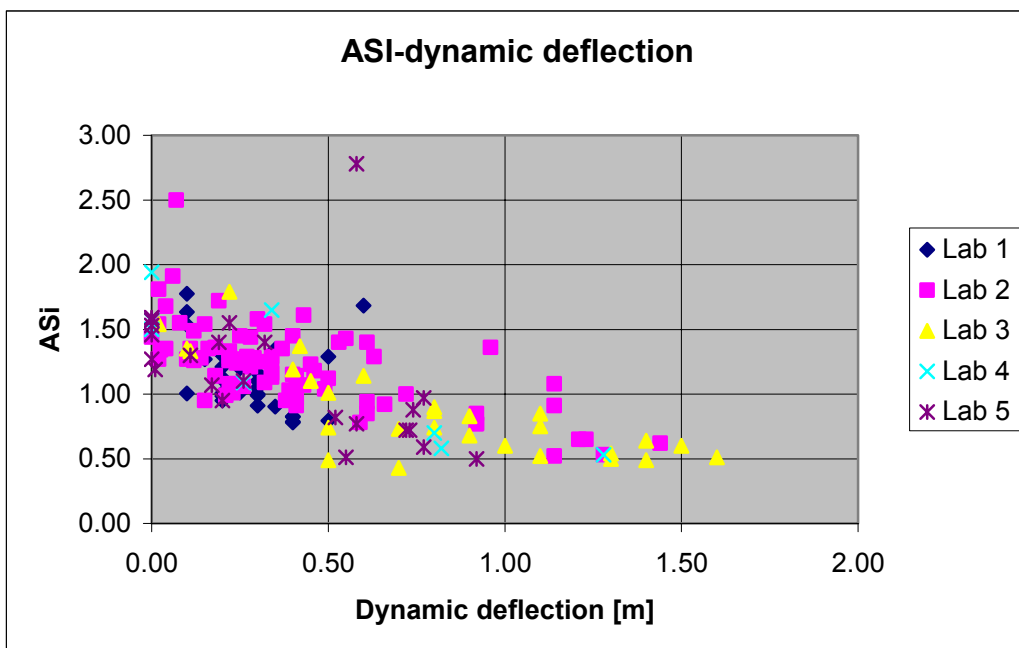


Figure 9: ASI and dynamic deflection correlation at different laboratories.

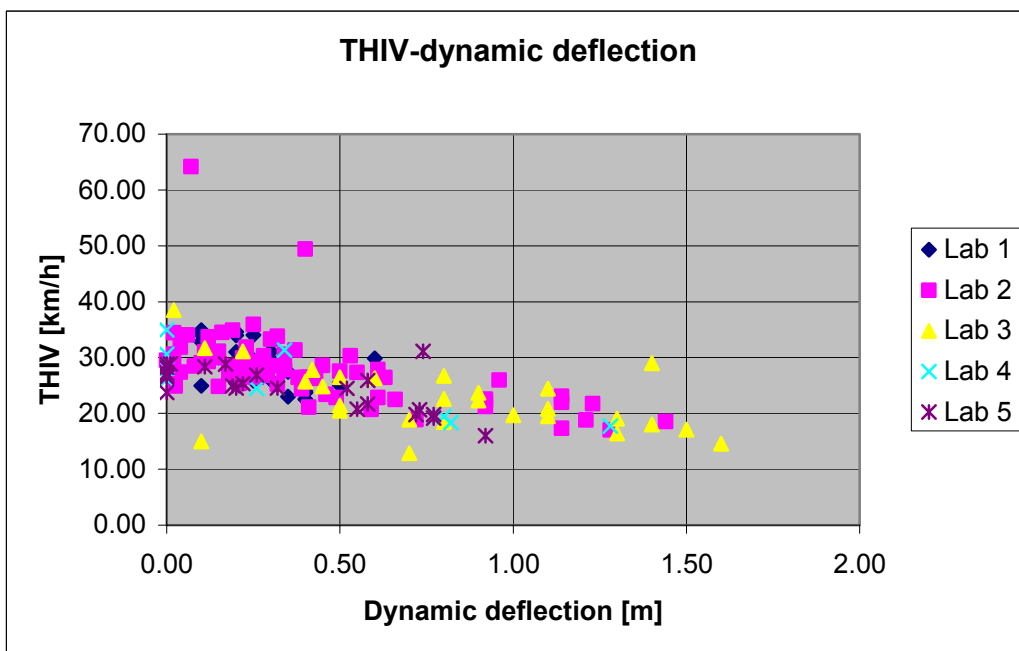


Figure 10: THIV and dynamic deflection correlation at different laboratories

From Figure 9 and Figure 10 it can be seen that the tendencies of these results are the same in all the laboratories. In the following table the correlation functions of different laboratories are reported. The differences between the correlation functions for Labs 4 and 5 are probably due to the small number of tests provided.

Lab	Corr. Function
All	$y = 1.4448e-0.683x$
1	$y = 1.2829e-0.5836x$
2	$y = 1.4973e-0.6099x$
3	$y = 1.3841e-0.6902x$
4	$y = 1.6442e-0.9867x$
5	$y = 1.4716e-0.8779x$

Table 5: ASI-DD correlation function

Lab	Corr. Function
All	$y = 30.631e-0.3764x$
1	$y = 32.827e-0.5464x$
2	$y = 32.141e-0.4018x$
3	$y = 27.476e-0.2846x$
4	$y = 29.923e-0.4634x$
5	$y = 27.801e-0.3747x$

Table 6: THIV-DD correlation function

3 Analysis of existing raw data

3.1 Introduction

Inside Work Package 3 of ROBUST, techniques have been used to evaluate the severity indices and a problem related to the moving average used inside ASI and PHD has been identified.

The current definition of the ASI index includes the application of a moving average over 50 milliseconds to the acceleration data. The origin of this calculation procedure was based on research on the injury assessment of vehicle and aircraft occupants in phenomena such as re-entry space capsule impacts, combat airplane manoeuvres, and traversing slope embankments. These phenomena were deemed to have a common duration of less than 50 ms, or, if duration was longer, limited oscillations throughout the event. For this reason, computing an average over a period of 50 ms was used to obtain an average value to be compared with the tolerable limits.

Impacts against road restraint systems generally have a duration greater than 50 milliseconds, and show strong oscillations at different frequencies. For this reason, it is not completely justified that the above mentioned severity criteria can provide precise injury assessment. Also, the 50 ms moving average when applied over long acceleration pulses becomes a low-pass filter, but it does not behave like filters used conventionally for crash analysis.

From the point of view of calculus, the analysis of the ASI procedure has shown that the moving average used inside the ASI and PHD evaluations does not perform like a regular low-pass filter. A new procedure to evaluate the ASI value has been proposed. This new procedure uses a standard filtering technique instead of the moving average.

One of the problems that must be solved is the choice of the cut off frequency for this filtering. The objective of this part of the project was to find an answer to this problem by applying the modified version of the ASI formula to the database of raw data obtained from the test houses.

3.2 Raw data

The raw data contained acceleration data in the three directions (x, y, and z) and yaw rate from TB11 tests. To guarantee anonymity no further information has been acquired on the tests.

3.3 Analysis of raw data

The set of data has been analysed by comparing the ASI evaluated with the standard method currently within EN1317-1, with a new ASI evaluated calculated using a standard filtering technique (instead of the moving average).

Standard ASI:

The acceleration severity index ASI is a function of time, computed with the following equation (1):

$$ASI(t) = \left[(\bar{a}_x / \hat{a}_x)^2 + (\bar{a}_y / \hat{a}_y)^2 + (\bar{a}_z / \hat{a}_z)^2 \right]^{1/2} \quad (1)$$

where :

\hat{a}_x , \hat{a}_y and \hat{a}_z are the limit values for the components of the acceleration along the body axis x, y and z;

$$\hat{a}_x = 12g, \hat{a}_y = 9g, \hat{a}_z = 10g, \quad (2)$$

\bar{a}_x , \bar{a}_y and \bar{a}_z are the components of the acceleration of a selected point P on the vehicle, filtered with a CFC180 filter (refer to ISO 6487 for further information) and averaged over a moving time interval $\delta = 50$ ms, so that:

$$\bar{a}_x = \frac{1}{\delta} \int_t^{t+\delta} a_x dt; \quad \bar{a}_y = \frac{1}{\delta} \int_t^{t+\delta} a_y dt; \quad \bar{a}_z = \frac{1}{\delta} \int_t^{t+\delta} a_z dt; \quad (3)$$

$g = 9,81 \text{ ms}^{-2}$ and is the value for acceleration due to gravity.

$$ASI = \max [ASI(t)] \quad (4)$$

Modified ASI:

The modified ASI is a function of time, computed with the following equation (5):

$$ASI(t) = \left[(\bar{a}_x / \hat{a}_x)^2 + (\bar{a}_y / \hat{a}_y)^2 + (\bar{a}_z / \hat{a}_z)^2 \right]^{1/2} \quad (5)$$

where:

\hat{a}_x , \hat{a}_y and \hat{a}_z are the limiting values for the components of acceleration along the body axis x, y and z;

$$\hat{a}_x = 12g, \hat{a}_y = 9g, \hat{a}_z = 10g, \quad (6)$$

\bar{a}_x , \bar{a}_y and \bar{a}_z are the components of the acceleration of a selected point P of the vehicle, filtered first with a CFC180 filter and then with a 2-pole Butterworth filter (forward and backward to avoid time shift) to create a resultant 4-pole filter (CFC shaped filter).

$g = 9,81 \text{ ms}^{-2}$ is the reference for the acceleration.

$$ASI = \max [ASI(t)]$$

3.4 Butterworth filter

The filter proposed instead of the moving average is a 4-pole phase-less digital filter defined, for a specific cut-off frequency, by the following equations in the time domain:

$$X(t) = \text{input signal}$$

$Y(t)$ = filtered signal

T = sampling period

CF = cut off frequency

- According to ISO 6487, the value of CF to be introduced in this equation is the cutoff frequency at -6dB, which equals 1,25 times the cutoff frequency at -3dB. Hence, the filters used in the study are defined by their cutoff frequency at -6dB.
- According to ISO 6487, the value of CF is not the same as the CFC class value for a filter. For example, for CFC 180, the cutoff frequency at -3dB is 300, and the cutoff frequency at -6dB to be introduced in the equation is $300 \cdot 1.25 = 375$.

The filtered signal is defined by:

$$Y(t) = a_0 X(t) + a_1 X(t-1) + a_2 X(t-2) + b_1 Y(t-1) + b_2 Y(t-2) \quad (7)$$

Where:

$$w_d = 2 \cdot \pi \cdot CF$$

$$w_a = \sin(w_d \cdot T / 2) / \cos(w_d \cdot T / 2)$$

$$a_0 = w_a^2 / (1.0 + \sqrt{2} \cdot w_a + w_a^2)$$

$$a_1 = 2 \cdot a_0$$

$$a_2 = a_0$$

$$b_1 = -2(w_a^2 - 1) / (1 + \sqrt{2} \cdot w_a + w_a^2)$$

$$b_2 = (-1 + \sqrt{2} \cdot w_a - w_a^2) / (1 + \sqrt{2} \cdot w_a + w_a^2)$$

Equation 7 is for a 2-pole filter. To obtain a 4-pole filter, signals are passed through the filter twice. The first time the signal is passed through in the forward direction, the second time in the rearwards direction (to cancel the time shift).

It has to be noted that even if this filter has been defined as a “CFC shaped filter”, the value of this CF (e.g., 12 Hz) does not correspond to the filter “CFC 12”

3.5 Results

The method described above has been applied to the available set of raw data to investigate the influence of different cut off frequencies on the results and to identify the most appropriate cut off frequency.

The following figure contains ASI values obtained with the standard technique (shown in dark blue and labelled ‘ASI’) and those calculated with the modified technique with different cut off frequencies from 10 Hz up to 20 Hz. Linear regressions are also reported.

In Appendix 2 the same results are reported in a tabular format.

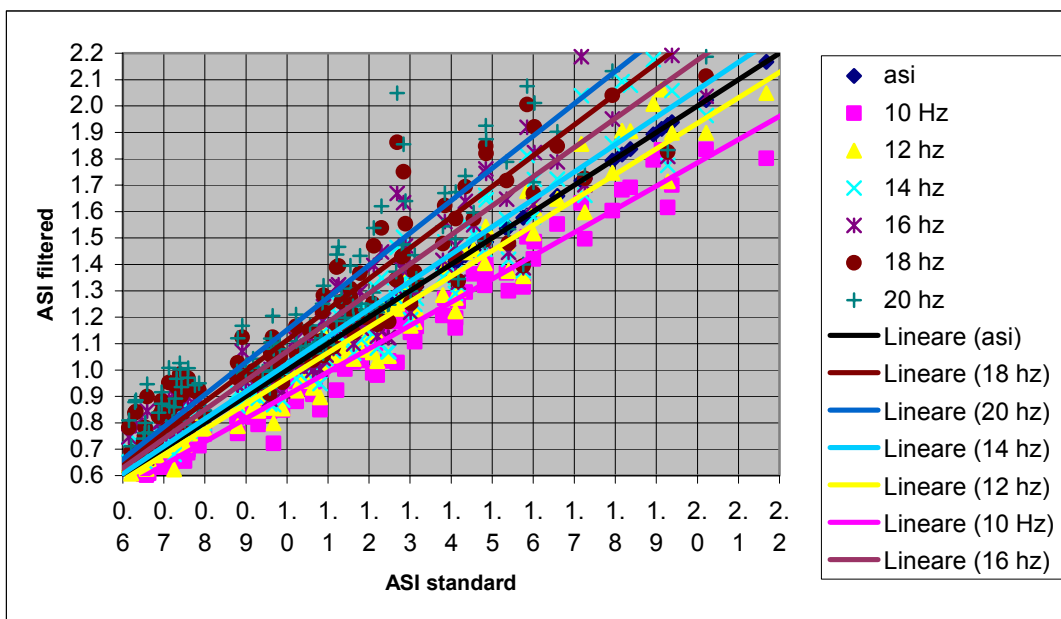


Figure 11: Comparison between ASI standard and modified ASI

By changing the cut off frequency, the modified ASI follows this change and the modified ASI value increases with an increase in the cut off frequency.

The final cut off frequency (12 Hz) has been identified as the one that has the best correlation with the current standard ASI formula. The objective is to avoid, if possible, modification of the current limits for the ASI formula.

The following figure shows the correlation between standard ASI and modified ASI using the above filtering technique with a 12 Hz cut off frequency.

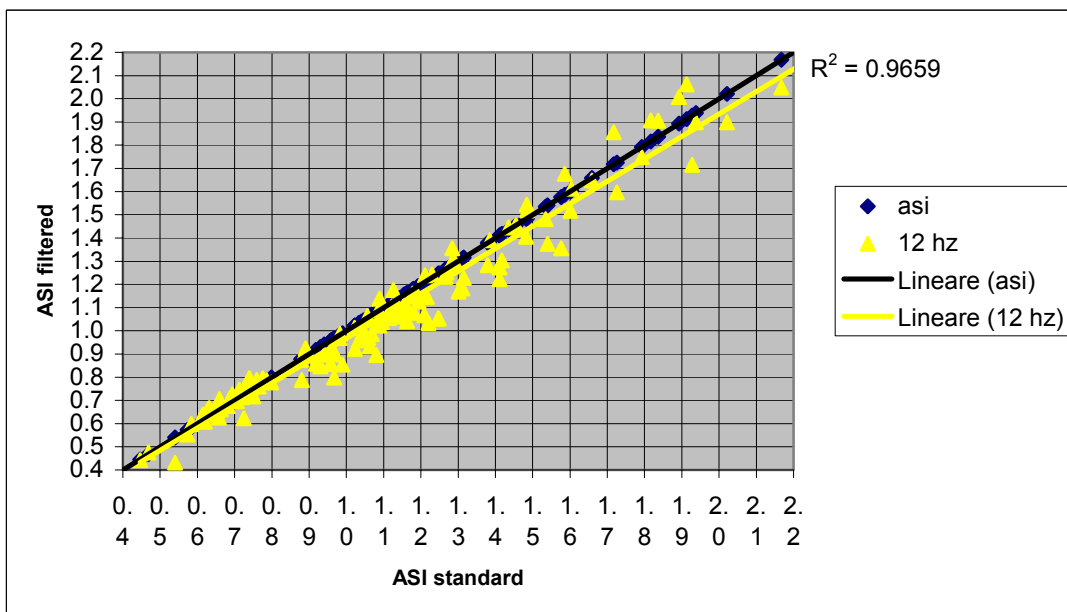


Figure 12: Comparison between standard ASI and modified ASI at 12 Hz

It can be seen that globally the tendency is similar between the two sets of ASI results, but some ASI values are decreased whilst some others are increased.

In any case, implementing this procedure implies that the values of the severity indices would suffer variations that may affect their classification according to the current EN 1317.

In general we can see a smaller influence on low values of ASI and a stronger influence on higher ASI values. This is probably related to the strong oscillations that are present in impacts with high ASI values which are filtered insufficiently by the moving average method.

It must be also be noted that if we perform the same statistical analysis but divide the population into different ranges of ASI, it can be seen that the most critical values (ASI from 1.0 to 1.4) are not the ones which best correspond to the 12 Hz filter (See figures).

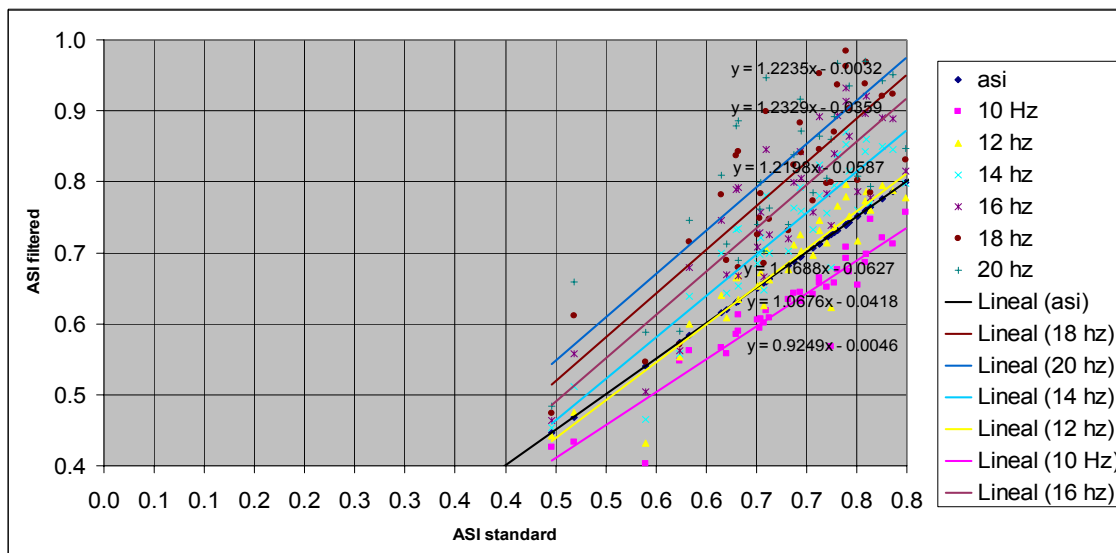


Figure 13 ASI (0 – 0.8). Very good agreement to a cut-off frequency 12 Hz.

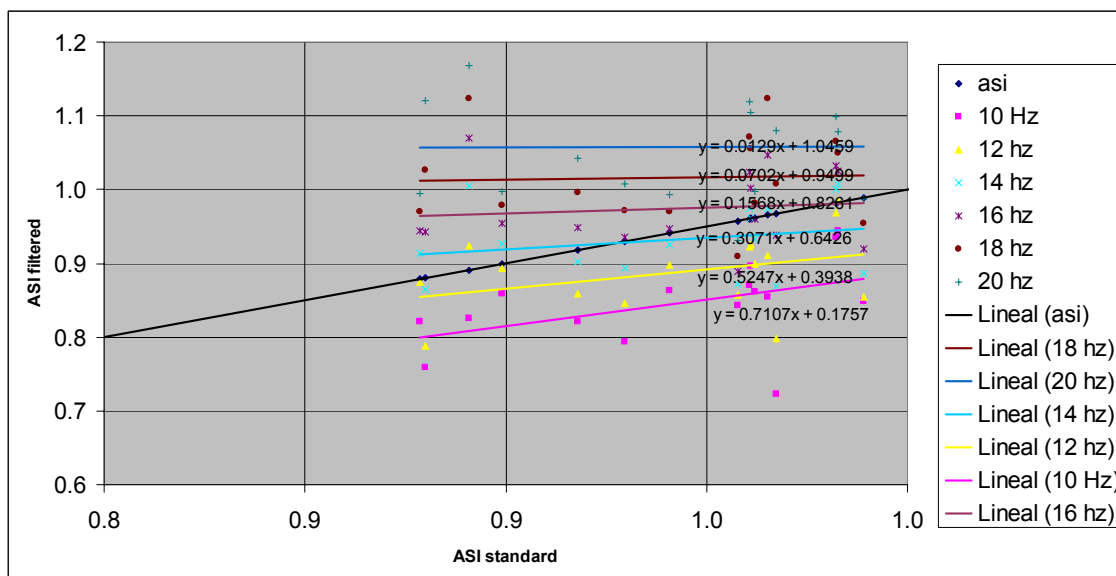


Figure 14. (ASI 0.8 – 1.0). 12 Hz cut-off frequency slightly underpredicting. Note: Small slopes in linear functions

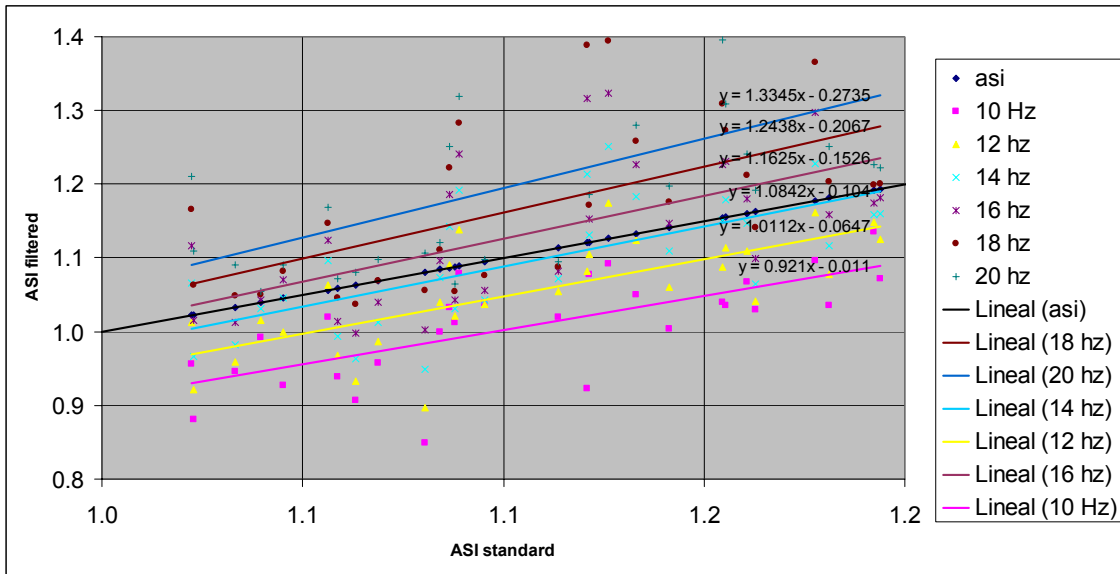


Figure 15. (ASI 1.0 – 1.2). 12 Hz cut-off frequency slightly underpredicting

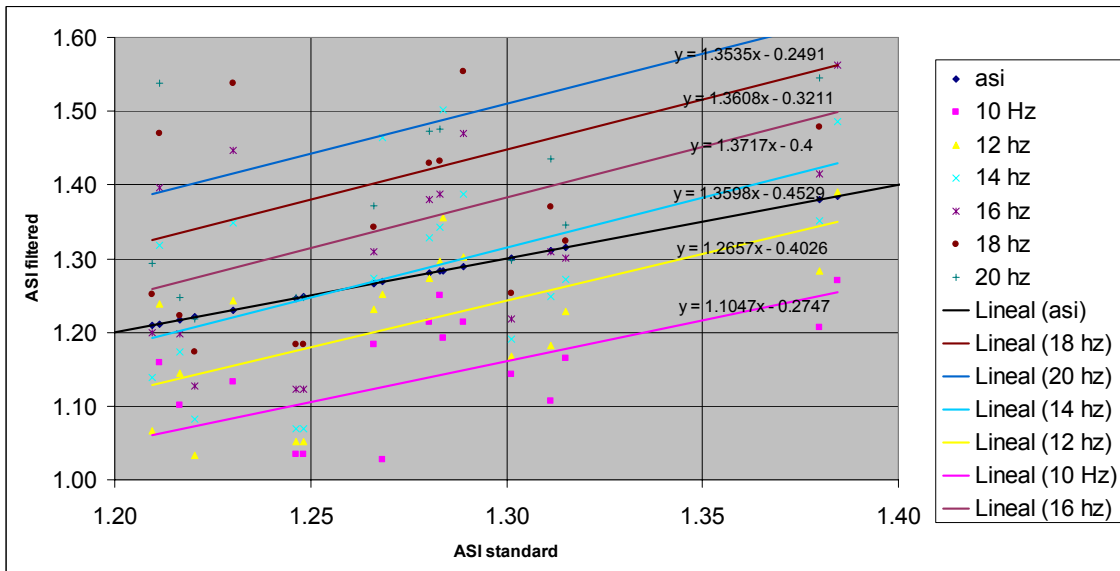


Figure 16. (ASI 1.2 – 1.4). 12 and 14 Hz cut-off frequencies show the best agreement.

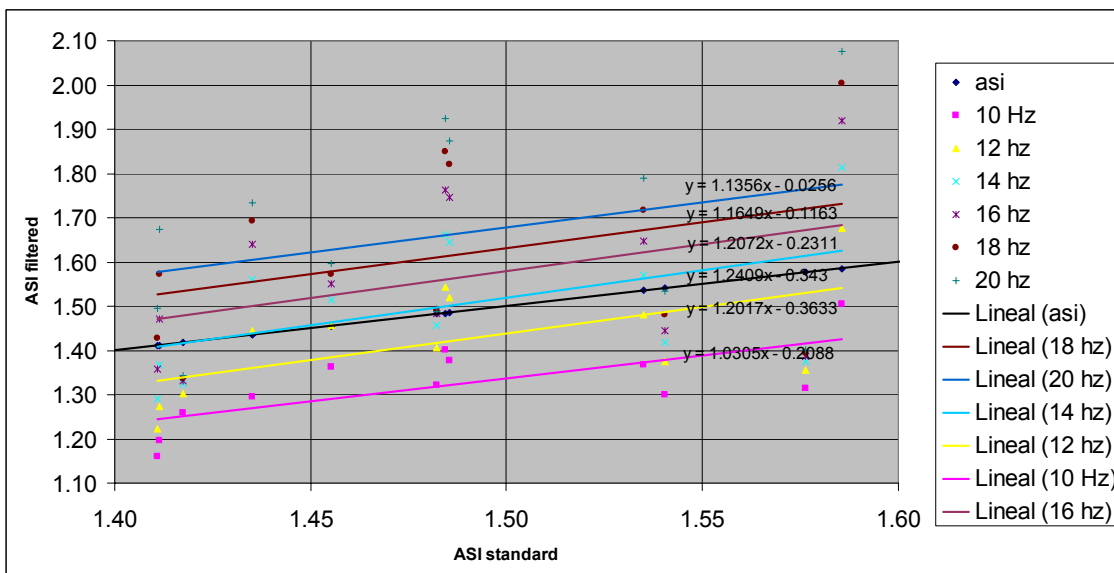


Figure 17. (ASI 1.4 – 1.6). 12 and 14 Hz cut-off frequencies show the best agreement.

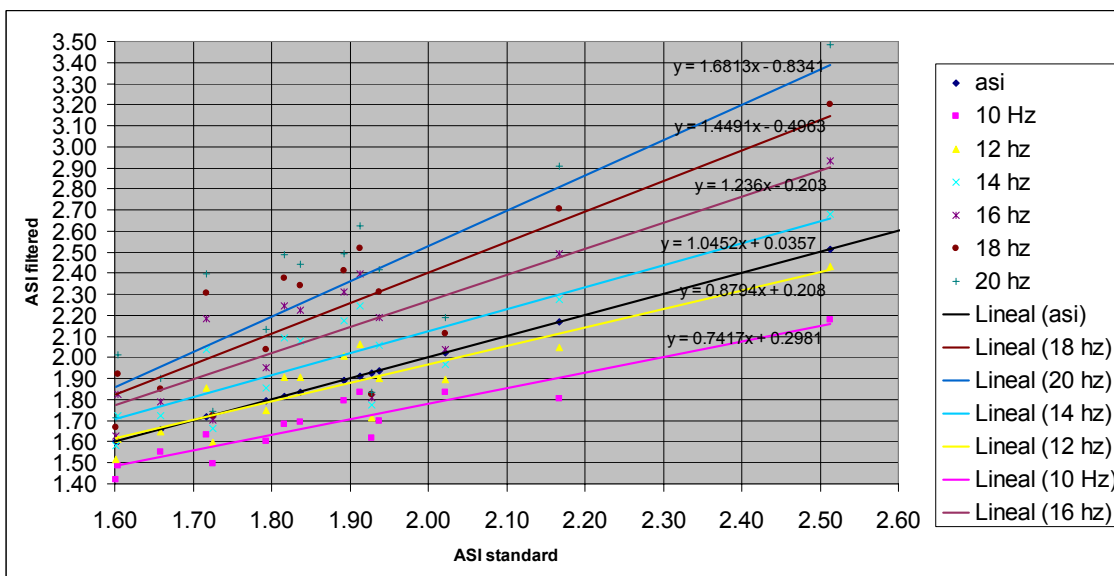


Figure 18.(ASI 1.6). 12 and 14 Hz cut-off frequencies show the best agreement.

4 Correlation between barrier performance and biomechanics criteria

EN 1317 should evaluate barrier performance using standard tests. This evaluation procedure contains the use of severity indices (ASI, THIV). Experience has shown that by using these evaluation procedures, barrier performance has strongly improved since the introduction of EN1317.

One of the proposals that the ROBUST project has evaluated is the use of injury criteria from instrumented dummies as an alternative to severity indices for the evaluation of barrier performance.

For this purpose, biomechanical and vehicle data from TB11 tests that included a Hybrid III instrumented dummy were collected and analysed. The data acquired were:

- Vehicle centre of gravity acceleration and yaw rate time histories
- Neck load time histories
- Dummy head acceleration time histories.

None of the tests failed the neck criteria for a purely frontal impact.

In the following table, severity indices and HIC values for 23 tests are reported.

Test	ASI traditional	THIV	time of flight	PHD	HIC
		m/s	s	g	
34	1.266	31.396	0.205	12.441	4397.334
90	0.961	24.278	0.266	20.035	2615.130
58	1.181	33.238	0.165	16.609	2168.279
82	1.246	26.513	0.188	19.176	808.003
65	1.221	28.131	0.400	14.998	797.722
85	1.023	22.920	0.200	13.724	264.725
59	1.178	31.732	0.412	13.428	173.480
81	1.088	27.017	0.186	20.570	158.436
32	1.385	26.726	0.301	9.266	109.335
63	0.880	20.968	0.207	22.486	97.299
60	1.535	31.954	0.362	18.937	73.995
62S	0.965	23.405	0.406	25.880	66.324
86	1.022	22.632	0.197	16.416	60.497
87	0.899	25.590	0.192	11.183	60.046
64S	1.284	23.603	0.328	10.693	55.435
93	0.764	21.935	0.201	9.176	52.242
84	1.095	28.715	0.184	12.967	50.105
89	0.958	25.306	0.195	13.841	49.394
88	1.089	27.796	0.179	9.547	41.355
92	0.941	23.710	0.196	6.569	37.238

91	0.918	23.613	0.249	17.446	29.300
18	0.879	21.043	0.204	15.383	11.680
61S	0.540	13.764	0.447	12.156	8.660

- 3 of 23 tests had HIC values exceeding the limit of 1000.
- In some cases the HIC value was greater than twice the 1000 limit, indicating a very severe impact.
- In some cases a high THIV value was recorded, however these tests would have failed in any case due to non-compliance with other test parameters.

The above table is also reported in the following figures comparing ASI and THIV to HIC values:

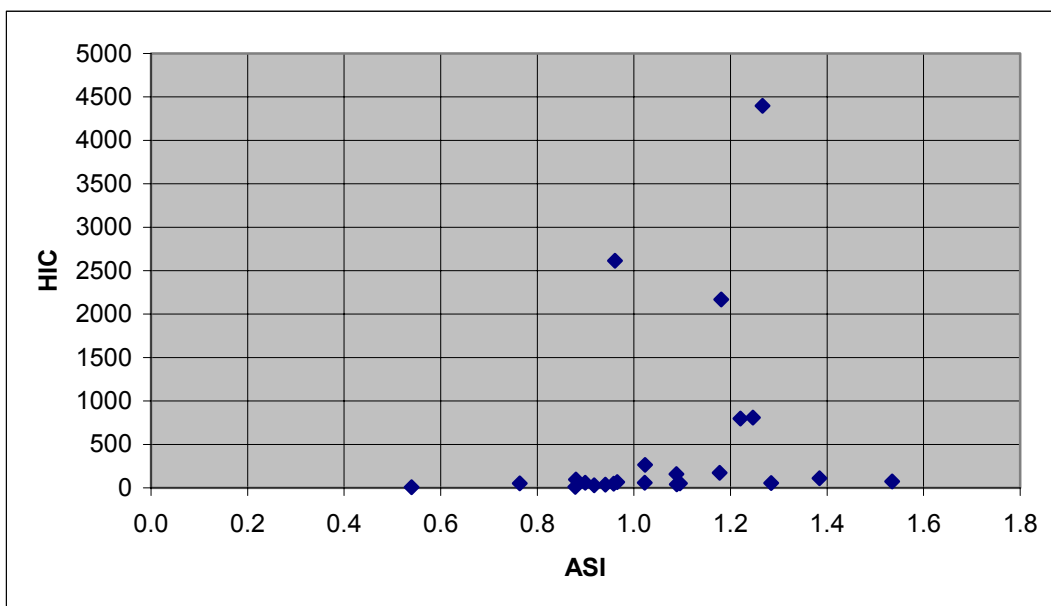


Figure 19: ASI and HIC correlation

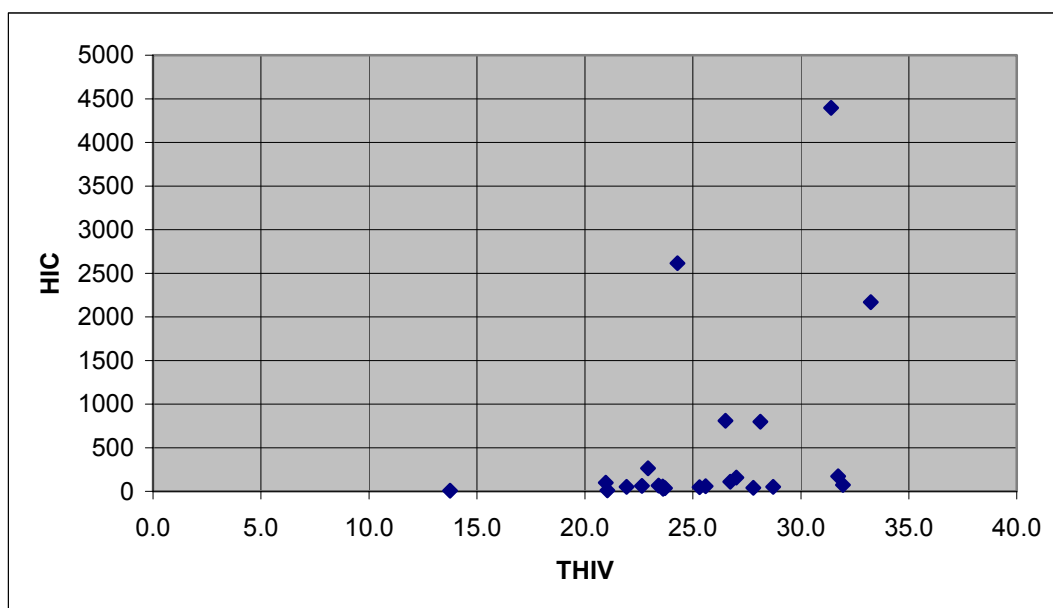


Figure 20: THIV and HIC correlation

The following observations can be made.

- The size of the data set is not statistically large enough to draw any final conclusions.
- EN1317-2 tests are fronto-lateral impacts and currently no specific dummies are available for this type of impact. Tests have only been performed with Hybrid III dummies and these have been developed for frontal-only impacts.
- When analysing the HIC criterion, even very 'bad' barriers produced very low injury criteria for the dummy measurements.
- A high value of HIC can only be seen if there is a direct impact between the head of the dummy and the barrier (this can be seen with other methods).
- Dummy measurements can be heavily influenced by differences in the vehicle behaviour and structure.
- Severity indices are used to rank and compare barrier performances; they are not to give a direct measure of the risk of injuries.
- Other dummy-based injury criteria that are used in crash safety, such as chest deflection, lumbar spine loads, etc. were not analysed in this task due to unavailability of data.

These observations lead to the conclusion that, at present, dummies should not be used to evaluate the performance of a barrier in isolation.

The use of dummy measurements in the evaluation of barrier performance, impact severity and ranking (EN1317 scope) is not suggested.

The acquisition of relevant dummy data is suggested so as to acquire information for future revisions of EN1317.

An appropriate dummy could be used to verify head impacts with the barrier. This could later become a fail criterion for future tests.

Appendix 1

In this Appendix, the table used for the correlation analysis is reported in an anonymous format.

Speed	Angle	Dyn Deflection	Sampling Rate	ASI	THIV	PHD
93.6	20.0	0.25	2500.00	1.02	26.29	11.32
99.08	20.0	0.15	2500.00	1.27	30.02	15.83
99.36	20.0	0.40	2500.00	0.78	23.74	12.73
99.43	20.0	0.50	2500.00	1.29	25.52	7.93
99.72	20.0	0.40	2500.00	0.79	23.76	14.02
99.72	20.0	0.20	2500.00	0.95	25.37	12.27
99.77	20.0	0.29	10000.00	1.28	26.81	12.45
99.98	20.0	0.10	2500.00	1.54	34.07	9.77
100	20.0	0.25	2500.00	1.01	25.87	19.28
100.00	21.0	0.80	2000.00	1.31	32.00	16.90
100.03	20.0	0.60	2500.00	1.68	29.86	8.77
100.08	20.0	0.40	2500.00	0.82	22.55	11.67
100.08	20.0	0.30	2500.00	0.91	26.00	12.75
100.08	20.0	0.25	2500.00	1.20	34.01	19.71
100.08	20.0	0.20	2500.00	1.30	33.98	11.28
100.10	21.0	0.34	16000.00	1.65	31.32	15.90
100.11	20.0	0.50	10000.00	1.12	27.56	14.34
100.19	20.0	0.39	10000.00	1.03	24.36	21.91
100.22	20.0	0.21	10000.00	0.99	25.36	15.42
100.39	20.0	0.11	10000.00	1.35	31.02	19.08
100.40	19.50	0.80	16000.00	0.70	19.44	5.70
100.4	20	0.19	10000.00	1.4	24.912	
100.41	20.0	0.22	10000.00	1.08	28.24	20.04
100.44	20.0	0.40	2500.00	0.83	23.95	14.36
100.44	20.0	0.35	2500.00	0.90	23.01	17.63
100.44	20.0	0.25	2500.00	1.04	29.57	11.03
100.44	20.0	0.30	2500.00	1.16	31.13	14.25
100.44	20.0	1.14	10000.00	0.52	17.30	10.32
100.50	20.0	0.32	10000.00	1.09	25.23	18.23
100.53	20.0	0.02	10000.00	1.54	30.61	10.39
100.60	20.0	0.26	10000.00	1.09	24.48	6.90
100.61	20.0	0.55	10000.00	1.43	27.36	18.32
100.75	20.0	0.40	10000.00	1.45	49.39	26.51
100.79	20.0	0.10	2500.00	1.78	32.81	10.57
100.8	20.0	0.30	2500.00	1.00	29.70	8.35
100.8	20.0	0.20	2500.00	1.11	34.59	13.93
100.80	20.0	1.28	20000.00	0.53	17.73	4.92
100.80	20.0	0.00	10000.00	1.57	30.60	8.80
100.8	20	0.01	10000.00	1.19	28.908	
100.81	20.0	0.32	10000.00	1.54	33.81	16.64
100.90	20.0	0.82	16000.00	0.58	18.36	4.90

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101.00	20.0	0.34	10000.00	1.29	28.22	19.89
101.00	20.0	0.00	10000.00	1.94	34.92	8.00
101.01	20.0	0.72	10000.00	1.00	18.88	18.33
101.06	19.9	0.22	10000.00	1.26	29.75	23.41
101.15	20.0	0.00	10000.00	1.44	29.49	5.68
101.16	20.0	0.30	2500.00	0.99	29.52	9.88
101.16	20.0	0.20	2500.00	1.01	29.24	9.56
101.20	20.0	1.44	10000.00	0.62	18.53	13.35
101.20	20.0	0.23	10000.00	1.27	31.87	20.64
101.20	21.0	1.04	10000.00	0.55	18.70	4.20
101.29	20.0	0.12	10000.00	1.26	29.27	12.77
101.32	20.0	0.10	2500.00	1.01	24.93	10.37
101.4	20	0	10000.00	1.53	28.224	
101.5	20.0	0.20	2500.00	1.13	27.78	17.93
101.52	20.0	0.20	2500.00	0.98	28.92	12.68
101.52	20.0	0.30	2500.00	1.05	28.12	21.18
101.52	20.0	0.49	10000.00	1.04	22.81	15.98
101.52	20.0	0.02	10000.00	1.27	27.98	13.46
101.52	20.0	0.22	10000.00	1.33	29.89	29.51
101.52	20.0	0.15	10000.00	1.54	31.11	11.00
101.55	20.7	0.41	10000.00	1.14	26.47	12.77
101.60	20.0	0.59	10000.00	0.78	20.68	13.70
101.60	20.0	0.63	10000.00	1.29	26.40	8.06
101.6	20	0.2	10000.00	0.95	24.516	
101.66	20.0	1.21	10000.00	0.65	18.80	11.69
101.66	20.0	0.22	10000.00	1.26	27.83	23.63
101.66	20.0	0.96	10000.00	1.36	25.96	9.07
101.69	20.0	1.14	10000.00	0.91	23.03	19.97
101.72	20.2	0.38	10000.00	0.95	26.42	9.84
101.80	20.0	0.92	10000.00	0.85	22.23	14.19
101.80	20.0	0.07	10000.00	2.50	64.18	46.68
101.83	20.0	0.26	10000.00	1.06	26.42	24.61
101.83	20.0	0.22	10000.00	1.29	29.22	16.67
101.88	20.0	0.30	2500.00	1.10	28.17	15.15
101.88	20.0	0.35	2500.00	1.35	27.45	28.85
101.89	20.0	0.92	10000.00	0.77	22.53	16.33
101.95	20.0	0.15	10000.00	0.95	24.82	13.71
101.95	19.9	0.18	10000.00	1.14	28.54	20.37
101.95	20.0	0.30	10000.00	1.58	33.30	30.14
101.98	20.0	0.40	10000.00	1.15	26.41	23.86
102.00	20	0.5	8000.00	0.49	21.40	4.00
102.00	20	1.0	12500.00	0.6	19.70	5.80
102.00	20	1.1	12500.00	0.85	24.40	14.70
102.01	20.0	0.66	10000.00	0.92	22.50	23.06
102.06	20.0	0.61	10000.00	1.40	27.87	9.11
102.09	19.9	0.61	10000.00	0.94	26.61	20.17
102.18	20.0	0.23	10000.00	1.01	26.72	20.56
102.18	20.0	0.03	10000.00	1.34	24.86	14.91
102.2	20	0.58	10000.00	2.78	25.92	
102.21	20.0	0.53	10000.00	1.40	30.29	12.30
102.24	20.0	0.20	2500.00	1.21	30.99	12.29

102.24	20.1	0.61	10000.00	0.85	22.82	16.42
102.24	19.9	0.41	10000.00	0.97	26.37	18.47
102.3	20	0.55	10000.00	0.51	20.736	
102.3	20	0.92	10000.00	0.5	16.02	
102.4	20	0.73	10000.00	0.72	20.628	
102.41	20.0	0.43	10000.00	1.61	26.34	11.40
102.44	20.0	0.41	10000.00	0.91	21.12	13.86
102.47	20.0	0.18	10000.00	1.14	27.30	8.06
102.50	20.0	0.12	10000.00	1.49	33.70	19.19
102.56	20.0	0.43	10000.00	1.07	26.23	27.87
102.68	20.0	0.46	10000.00	1.18	23.38	9.23
102.7	20	0	10000.00	1.27	23.76	
102.71	20.0	1.23	10000.00	0.65	21.75	11.99
102.71	20.0	0.37	10000.00	1.35	31.32	10.08
102.71	20.0	0.28	10000.00	1.44	30.33	30.40
102.73	20.0	0.18	10000.00	1.36	27.35	11.48
102.73	20.0	0.19	10000.00	1.72	34.89	18.21
102.8	20	0	10000.00	1.46	26.784	
102.85	20.0	0.02	10000.00	1.81	34.41	12.53
102.91	20.0	0.28	10000.00	1.21	29.18	14.72
103.00	19	1.4	8000.00	0.49	18.00	4.30
103.00	20	0.1	8000.00	1.35	15.00	11.90
103.00	20.0	0.00	20000.00	1.57	28.08	14.20
103.06	20.0	0.27	10000.00	1.29	28.10	22.96
103.06	20.0	0.04	10000.00	1.35	27.40	9.85
103.06	20.0	0.16	10000.00	1.35	34.51	16.18
103.12	20.0	0.23	10000.00	1.08	26.49	22.99
103.12	19.7	0.24	10000.00	1.24	29.25	13.91
103.12	20.0	0.10	10000.00	1.27	29.03	15.98
103.2	20	0.26	10000.00	1.1	26.892	
103.2	20	0.77	10000.00	0.59	19.8	
103.2	20	0	10000.00	1.59	26.46	
103.21	20.0	0.14	10000.00	1.28	29.99	17.52
103.21	20.0	0.06	10000.00	1.91	34.02	13.86
103.24	20.0	0.45	10000.00	1.23	28.62	23.98
103.32	20.0	0.30	10000.00	1.25	28.51	21.00
103.4	20	0.77	10000.00	0.97	19.152	
103.4	20	0	10000.00	1.57	28.836	
103.4	20	0.17	10000.00	1.07	28.836	
103.50	20.0	0.00	20000.00	1.50	26.10	20.50
103.5	20	0.72	10000.00	0.72	19.8	
103.5	20	0.32	10000.00	1.4	24.552	
103.53	20.0	0.25	10000.00	1.45	35.92	26.98
103.6	20	0.74	10000.00	0.88	31.104	
103.65	20.0	0.34	10000.00	1.16	27.85	22.07
103.72	20.0	0.10	2500.00	1.64	34.87	6.45
103.8	20	0	10000.00	1.59	27.216	
103.9	20	0.11	10000.00	1.3	28.368	
104.00	20	0.9	10000.00	0.68	23.70	6.30
104.00	20	0.5	12500.00	1.1	24.80	9.90
104.00	20	0.0	10000.00	1.54	38.50	16.00

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104.01	20.0	0.08	10000.00	1.55	28.50	16.94
104.04	20.0	0.50	2500.00	0.79	25.01	15.15
104.04	20.0	1.14	10000.00	1.08	21.98	7.26
104.1	20	0.52	10000.00	0.82	24.48	
104.25	20.0	1.28	10000.00	0.53	17.02	14.02
104.34	20.0	0.34	10000.00	1.13	27.83	21.86
104.40	20.0	0.34	10000.00	1.24	30.55	24.99
104.4	20	0.58	10000.00	0.77	21.672	
104.6	20	0.22	10000.00	1.55	25.308	
104.80	20.0	0.92	10000.00	0.77	21.21	13.31
105.00	19	0.8	8000.00	0.87	22.60	7.80
105.00	20	0.4	12500.00	1.19	25.70	10.70
106	20	1.3	12500.00	0.5	16.4	4.50
106	19	1.6	8000.00	0.51	14.6	4.21
106.00	20	1.1	10000.00	0.52	19.50	4.40
106	19	1.3	8000.00	0.54	19.04	4.36
106.00	20	0.6	10000.00	1.14	26.30	10.50
106.00	20	0.4	12500.00	1.37	27.80	13.10
106.57	20.0	0.04	10000.00	1.68	31.83	14.52
107	20	1.4	10000.00	0.64	29	6.60
107.00	19	0.7	8000.00	0.73	18.90	6.50
107.00	20	0.8	12500.00	0.74	18.50	7.10
107.00	20	0.5	12500.00	0.74	20.50	6.50
107	20	1.1	12500.00	0.75	20.8	6.80
107	20	0.9	10000.00	0.83	22.3	7.30
107	20	0.8	10000.00	0.9	26.7	8.20
107.00	20	0.2	10000.00	1.79	31.10	17.90
108	20	0.1	10000.00	1.33	31.7	14.40
109.00	19	1.5	8000.00	0.6	17.10	4.96
110.00	19	0.7	8000.00	0.43	12.85	4.29
111.00	20	0.5	10000.00	1.01	26.50	9.10

Appendix 2

Standard ASI	Modified ASI					
	Cut off frequencies					
	10	12	14	16	18	20
0.446	0.427	0.442	0.454	0.464	0.474	0.484
0.469	0.434	0.475	0.511	0.558	0.611	0.659
0.540	0.403	0.431	0.465	0.504	0.546	0.588
0.573	0.548	0.553	0.558	0.562	0.570	0.589
0.584	0.562	0.599	0.639	0.679	0.715	0.745
0.615	0.566	0.640	0.699	0.746	0.782	0.810
0.620	0.558	0.608	0.643	0.668	0.690	0.712
0.630	0.585	0.665	0.732	0.789	0.837	0.878
0.632	0.612	0.635	0.653	0.668	0.679	0.689
0.632	0.590	0.667	0.734	0.792	0.842	0.886
0.651	0.605	0.653	0.685	0.708	0.726	0.740
0.653	0.594	0.654	0.698	0.728	0.748	0.761
0.655	0.606	0.672	0.722	0.758	0.783	0.800
0.658	0.601	0.626	0.647	0.667	0.685	0.702
0.660	0.618	0.705	0.780	0.845	0.900	0.946
0.663	0.608	0.661	0.699	0.726	0.747	0.763
0.682	0.634	0.676	0.703	0.720	0.731	0.739
0.688	0.643	0.711	0.763	0.799	0.823	0.838
0.694	0.644	0.726	0.791	0.843	0.884	0.916
0.695	0.632	0.703	0.759	0.804	0.841	0.872
0.706	0.641	0.696	0.733	0.757	0.773	0.785
0.712	0.657	0.746	0.823	0.892	0.953	1.007
0.713	0.665	0.731	0.781	0.818	0.845	0.864
0.721	0.652	0.713	0.756	0.783	0.798	0.805
0.725	0.568	0.623	0.680	0.739	0.799	0.859
0.728	0.657	0.736	0.795	0.839	0.870	0.892
0.731	0.676	0.765	0.838	0.894	0.936	0.967
0.739	0.709	0.797	0.871	0.932	0.984	1.026
0.739	0.691	0.779	0.852	0.913	0.962	1.002
0.743	0.673	0.752	0.815	0.864	0.904	0.936
0.751	0.654	0.717	0.760	0.787	0.801	0.808
0.759	0.686	0.773	0.842	0.897	0.938	0.970
0.760	0.697	0.787	0.860	0.920	0.968	1.007
0.764	0.747	0.760	0.769	0.778	0.785	0.793
0.776	0.721	0.795	0.850	0.891	0.920	0.942
0.786	0.712	0.787	0.845	0.889	0.923	0.950
0.799	0.757	0.778	0.798	0.815	0.831	0.847
0.879	0.822	0.875	0.914	0.945	0.970	0.994
0.880	0.760	0.787	0.864	0.943	1.027	1.120
0.891	0.826	0.924	1.005	1.070	1.124	1.168
0.899	0.858	0.894	0.927	0.955	0.978	0.998
0.918	0.821	0.859	0.902	0.948	0.996	1.043
0.930	0.794	0.846	0.893	0.935	0.972	1.007
0.941	0.863	0.898	0.925	0.948	0.970	0.994
0.958	0.844	0.857	0.872	0.889	0.910	0.932

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0.961	0.870	0.923	0.974	1.023	1.071	1.120
0.961	0.896	0.925	0.961	1.002	1.056	1.105
0.962	0.861	0.899	0.932	0.960	0.981	0.998
0.965	0.854	0.910	0.975	1.046	1.124	1.206
0.967	0.722	0.798	0.869	0.938	1.008	1.080
0.982	0.936	0.968	1.001	1.033	1.066	1.099
0.983	0.944	0.986	1.008	1.025	1.049	1.079
0.989	0.848	0.854	0.886	0.920	0.954	0.988
1.022	0.956	1.012	1.066	1.117	1.165	1.210
1.023	0.881	0.921	0.967	1.015	1.063	1.110
1.033	0.946	0.959	0.982	1.013	1.049	1.090
1.040	0.993	1.015	1.031	1.043	1.050	1.055
1.045	0.928	0.999	1.045	1.070	1.082	1.091
1.056	1.020	1.063	1.097	1.124	1.148	1.169
1.059	0.939	0.968	0.994	1.014	1.046	1.072
1.063	0.908	0.933	0.964	0.998	1.037	1.081
1.069	0.958	0.986	1.013	1.040	1.068	1.098
1.080	0.849	0.896	0.948	1.003	1.056	1.107
1.084	0.999	1.041	1.073	1.096	1.111	1.121
1.087	1.033	1.091	1.143	1.186	1.222	1.252
1.088	1.013	1.022	1.031	1.042	1.054	1.064
1.089	1.079	1.139	1.192	1.240	1.283	1.319
1.095	1.038	1.038	1.042	1.056	1.076	1.098
1.114	1.020	1.054	1.072	1.082	1.088	1.095
1.121	0.923	1.081	1.213	1.316	1.389	1.437
1.121	1.078	1.106	1.131	1.153	1.172	1.186
1.126	1.091	1.175	1.251	1.323	1.394	1.466
1.133	1.050	1.124	1.183	1.227	1.259	1.280
1.141	1.003	1.061	1.110	1.148	1.176	1.197
1.155	1.039	1.088	1.152	1.226	1.309	1.395
1.155	1.036	1.113	1.178	1.231	1.273	1.308
1.161	1.067	1.110	1.148	1.181	1.212	1.242
1.163	1.030	1.042	1.064	1.099	1.141	1.191
1.178	1.097	1.161	1.228	1.297	1.366	1.433
1.181	1.035	1.077	1.116	1.158	1.203	1.251
1.192	1.135	1.148	1.159	1.175	1.199	1.226
1.194	1.072	1.126	1.160	1.182	1.201	1.222
1.209	0.989	1.067	1.138	1.200	1.251	1.293
1.211	1.159	1.238	1.318	1.396	1.470	1.538
1.217	1.101	1.145	1.174	1.198	1.222	1.247
1.221	0.980	1.034	1.082	1.128	1.173	1.219
1.230	1.133	1.243	1.349	1.447	1.538	1.620
1.246	1.035	1.053	1.070	1.123	1.183	1.247
1.248	1.035	1.053	1.070	1.123	1.183	1.247
1.266	1.183	1.232	1.273	1.309	1.342	1.372
1.268	1.028	1.251	1.465	1.668	1.863	2.049
1.280	1.214	1.274	1.329	1.381	1.429	1.473
1.283	1.249	1.297	1.342	1.388	1.432	1.476
1.284	1.192	1.355	1.502	1.634	1.751	1.855
1.289	1.214	1.303	1.387	1.470	1.554	1.640
1.301	1.143	1.168	1.191	1.219	1.254	1.298

1.311	1.108	1.183	1.248	1.309	1.371	1.435
1.315	1.164	1.228	1.272	1.301	1.324	1.346
1.380	1.207	1.283	1.352	1.416	1.479	1.545
1.385	1.270	1.390	1.486	1.562	1.623	1.670
1.411	1.160	1.222	1.289	1.359	1.428	1.495
1.411	1.197	1.273	1.368	1.470	1.573	1.673
1.418	1.260	1.303	1.323	1.332	1.337	1.344
1.435	1.295	1.446	1.559	1.639	1.694	1.735
1.455	1.364	1.456	1.515	1.550	1.573	1.596
1.482	1.321	1.405	1.457	1.484	1.493	1.489
1.484	1.401	1.543	1.662	1.762	1.848	1.925
1.485	1.377	1.519	1.644	1.745	1.820	1.875
1.535	1.368	1.481	1.571	1.646	1.717	1.788
1.540	1.299	1.375	1.419	1.446	1.481	1.533
1.576	1.314	1.355	1.376	1.387	1.394	1.400
1.586	1.505	1.677	1.813	1.919	2.005	2.076
1.601	1.420	1.517	1.580	1.627	1.669	1.711
1.604	1.486	1.612	1.722	1.824	1.920	2.011
1.659	1.553	1.648	1.724	1.789	1.848	1.903
1.717	1.633	1.856	2.039	2.186	2.304	2.399
1.725	1.497	1.597	1.662	1.701	1.726	1.742
1.793	1.603	1.748	1.858	1.951	2.040	2.132
1.816	1.682	1.906	2.092	2.246	2.377	2.490
1.837	1.691	1.905	2.079	2.223	2.342	2.443
1.892	1.795	2.008	2.176	2.309	2.413	2.493
1.913	1.833	2.062	2.247	2.397	2.521	2.623
1.928	1.616	1.715	1.775	1.809	1.826	1.834
1.938	1.700	1.899	2.058	2.192	2.308	2.416
2.022	1.835	1.898	1.965	2.037	2.113	2.187
2.168	1.802	2.048	2.276	2.493	2.703	2.908
2.513	2.182	2.433	2.681	2.934	3.201	3.484